



Novelties coming in June 5.5 version

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www.localsolver.com



MSI株式会社 (日本総代理店)

Who we are



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<http://www.bouygues.com>

Innovation24

Operations Research subsidiary of Bouygues
20 years of practice and research

<http://www.innovation24.fr>

LocalSolver

Mathematical optimization solver
commercialized by Innovation 24

<http://www.localsolver.com>



LocalSolver

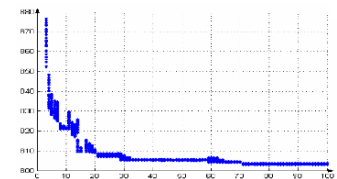
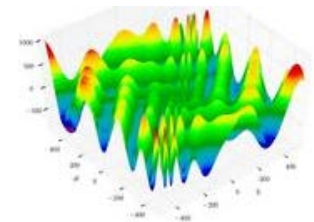
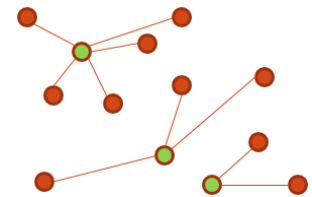
Hybrid math optimization solver

For combinatorial, numerical,
or mixed-variable optimization

Suited for large-scale
non-convex optimization

Quality solutions in seconds
without tuning

LocalSolver
=
LS+CP/ SAT+LP/ MP+NLP



Novelties

Innovative modeling concepts
for routing problems



Set-based modeling

Structured decisional operator `list(n)`

- Order a **subset** of values in domain $\{0, \dots, n-1\}$
- Each value is **unique** in the list

Classical operators to interact with “list”

- **count**(u): number of values selected in the list
- **at**(u,i) or `u[i]`: value at index i in the list
- **indexOf**(u,v): index of value v in the list
- **contains**(u,v): equivalent to “`indexOf(u,v) != -1`”
- **disjoint**(u1, u2, ..., uk): true if u1, u2, ..., uk are pairwise disjoint
- **partition**(u1, u2, ..., uk): true if u1, u2, ..., uk induce a partition of $\{0, \dots, n-1\}$



Traveling salesman

```
function model() {  
  x <- list(N) ; // order n cities {0, ..., n-1} to visit  
  constraint count(x) == N; // exactly n cities to visit  
  minimize sum[i in 1..N-1]( Dist[ x[i-1] ][ x[i] ] )  
    + Dist[ x[N-1] ][ x[0] ] ; // minimize sum of traveled distances  
}
```

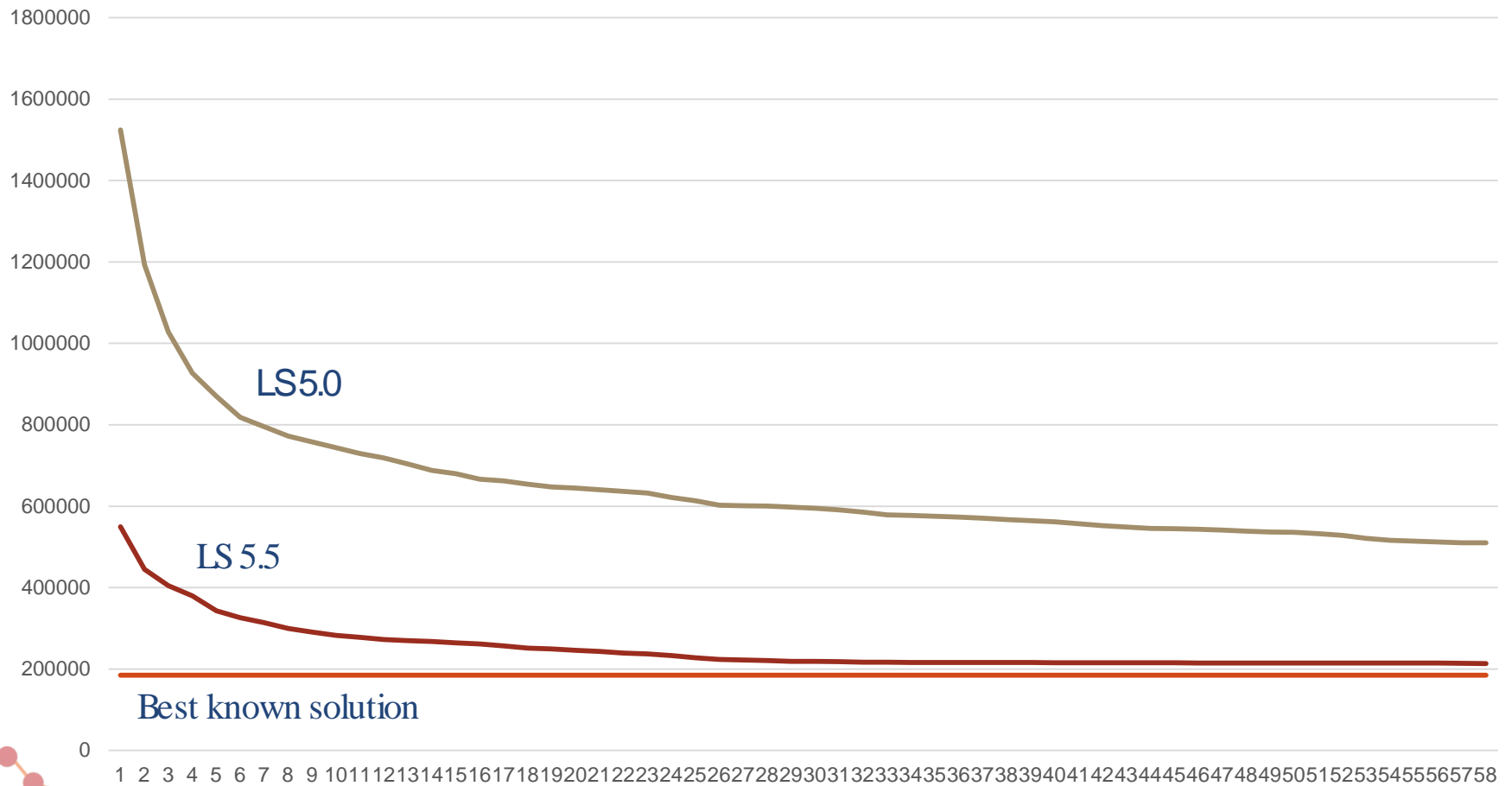
Could you imagine simpler model?

- Natural declarative model: straightforward to understand
- Common set-oriented concepts: easy to learn
- Still easier for people with (basic) programming skills
- Compact: linear in the size of input → highly scalable (1 million nodes)



Traveling salesman

TSP: real-life 200-client instance
LocalSolver 5.0 vs 5.5 (with operator *list*)



Vehicle routing

```
function model() {  
  x[1..K] <- list(N) ; // for each truck, order the clients to visit  
  constraint partition( x[1..K] ); // each client is visited once  
  distances[k in 1..K] <- sum[i in 1..N-1]( dist( x[k][i-1], x[k][i] )  
    + dist( x[k][N-1], x[k][0] ) ); // traveled distance for each truck  
  minimize sum[k in 1..K]( distances[k] ); // minimize total traveled distance  
}
```

To go further, to make it simpler

- Sets (unordered) versus lists (ordered)
- Multi-sets/lists: multiple occurrence of the same values
- Collections of objects instead of values
- Ability to iterate and project over collections (lambda expressions)



CVRP benchmarks

CVRP - instances A

- 32 to 80 clients, 10 trucks max.
- 27 instances
- 5 minutes of running time
- LS binary: almost infeasible
- **LS list: 1 % avg. opt. gap**

CVRP - instances X100-500

- 100 to 500 clients, 138 trucks max.
- 67 instances
- 5 minutes of running time
- LS binary: almost infeasible
- **LS list: 9 % avg. opt. gap**



CVRPTW- instances Solomon R100

- 101 to 112 clients, 19 trucks max.
- 13 instances
- 5 minutes of running time
- LS binary: N/A
- **LS list: 3 % avg. opt. gap**

CVRPTW- instances Solomon R200

- 201 to 208 clients, 4 trucks max.
- 8 instances
- 5 minutes of running time
- LS binary: N/A
- **LS list: 8 % avg. opt. gap**



Local Solver

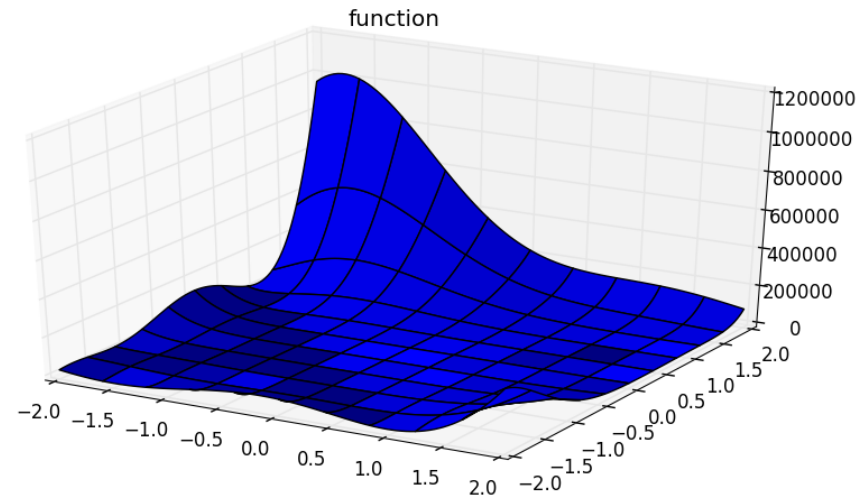
Black-box function optimization



Black-box optimization

Context

- Unknown objective (oracle)
- Costly to evaluate
- Derivative-free
- Continuous & integer decisions
- Bounds on decisions



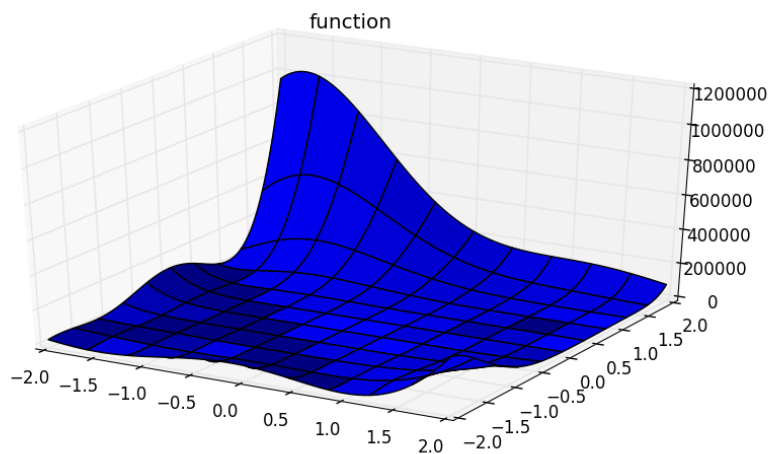
Many applications in engineering

- Multidisciplinary/parametric optimization
 - Simulation optimization (noisy, nondeterministic)
- Design optimization of materials/systems: mechanics, electricity, logistics, etc.

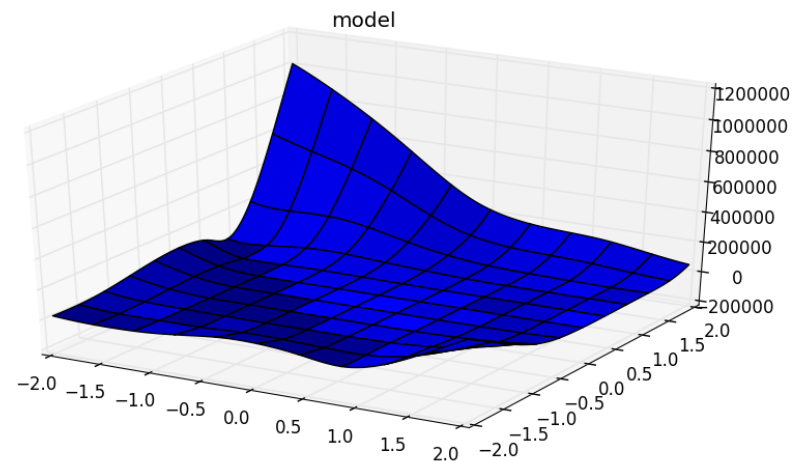


Learn the objective function landscape

- Objective landscape modeled by Radial Basis Functions
- Several models are built with different techniques/parameters
- Automatic selection of the most promising models for optimization



Objective Function

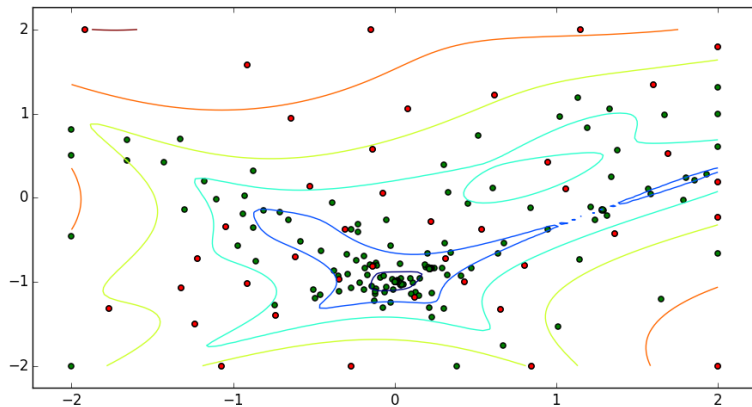


Objective Model

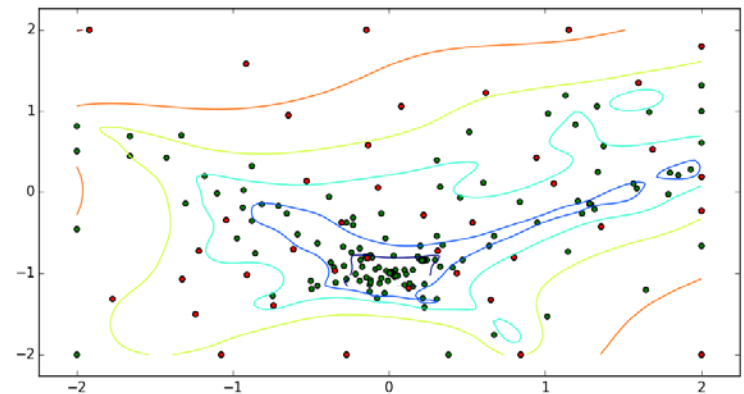


Exploitation & diversification

- Exploitation: optimize over the objective model
 - Diversification: explore new promising regions
- NLP subproblems solved through LocalSolver techniques:
local & direct search, gradient-based line search, etc.



Objective Function



Objective Model



Benchmark

Instances

- 25 instances from the recent paper by Costa and Nannicini.
RBFOpt: an open-source library for black-box optimization with costly function evaluations. Optimization Online. (under review)
- 20 runs per instance, 150 calls max. to the black-box per run
- Numerical precision: $1e-6$

Preliminary results

- RBFOpt: 345 opt. solutions found, 82 calls avg. per run
- **LocalSolver: 310 opt. solutions found, 94 calls avg. per run**
- NOMAD (GERAD): 170 opt. solutions found



Benchmark

Instance	LocalSolver			RBFOpt			NOMAD	
	#sol	Avg. Eval	Error (%)	#sol	Avg. Eval	Error (%)	#sol	Error (%)
branin	20	23	0,0	20	31	0,0	20	0,0
camel	20	26	0,0	20	34	0,0	19	4,0
ex_4_1_1	20	11	0,0	20	14	0,0	20	0,0
ex_4_1_2	20	51	0,0	20	9	0,0	20	0,0
ex_8_1_1	20	10	0,0	20	7	0,0	19	2,5
ex_8_1_4	20	44	0,0	20	25	0,0	0	341,5
gear	20	34	0,0	20	7	0,0	0	388,0
goldsteinprice	18	122	0,1	20	53	0,0	16	450,0
hartman3	8	130	1,2	20	45	0,0	15	9,4
hartman6	8	121	11,0	17	101	5,1	0	5,7
least	0	150	1308,0	0	150	204,7	0	129,0
nvs04	20	70	0,0	19	64	194,4	4	9997,0
nvs06	16	127	1,0	0	150	13,3	9	8,7
nvs09	20	15	0,0	20	14	0,0	16	1,2
nvs16	8	138	949,0	20	49	0,0	9	885,0
perm0_8	0	150	109,0	0	150	147,2	0	412,0
perm_6	0	150	2424958,0	0	150	44134,7	0	311032,0
rbrock	20	83	0,0	5	136	10,8	0	43,2
schoen_10_1	4	145	66,7	11	139	28,8	0	119,5
schoen_10_2	0	150	96,2	14	133	1,6	0	115,7
schoen_6_1	18	101	100,8	18	101	1,8	0	51,5
schoen_6_2	10	120	28,0	16	102	32,7	0	54,2
shekel10	8	118	29,6	13	107	60,1	0	56,9
shekel5	6	127	51,6	7	126	51,7	1	46,1
shekel7	6	127	28,5	5	137	47,0	2	47,9
	310			345			170	



John N. Hooker (2007)

“Good and Bad Futures for Constraint Programming (and Operations Research)”
Constraint Programming Letters 1, pp. 21-32

“Since modeling is the master and computation the servant, no computational method should presume to have its own solver.

This means there should be no CP solvers, no MIP solvers, and no SAT solvers. All of these techniques should be available in a single system to solve the model at hand.

They should seamlessly combine to exploit problem structure. Exact methods should evolve gracefully into inexact and heuristic methods as the problem scales up.”



LocalSolver

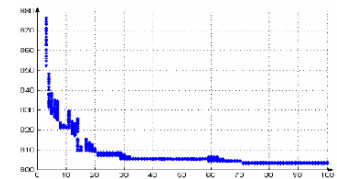
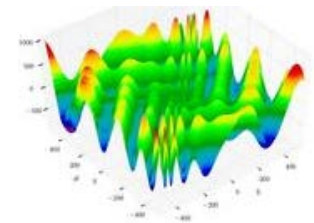
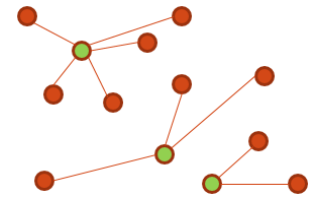
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free trial with support – free for academics - renting licenses
from 590 €/ month - perpetual licenses from 9,900 €

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